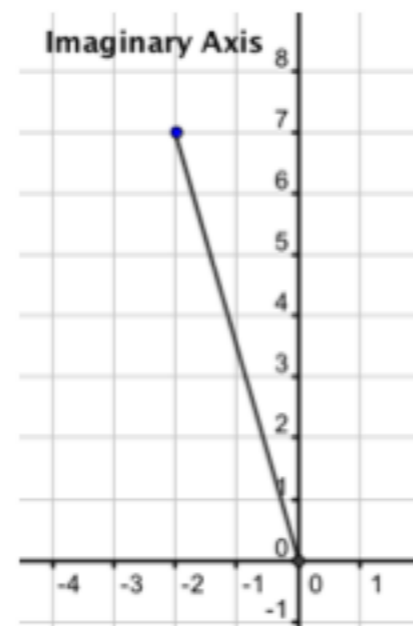


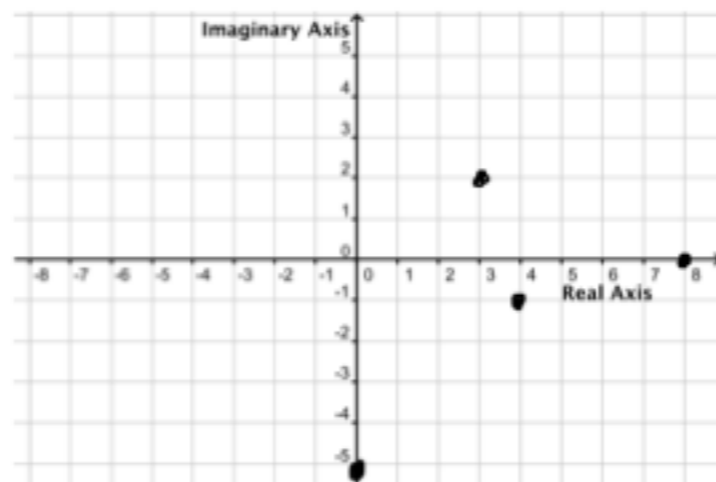
The x-y coordinate plane can be used to represent complex numbers, $a + bi$.
 The real part of the complex number, a , is represented by the x coordinate, and
 the imaginary part of the complex number, b , is represented by the y coordinate.



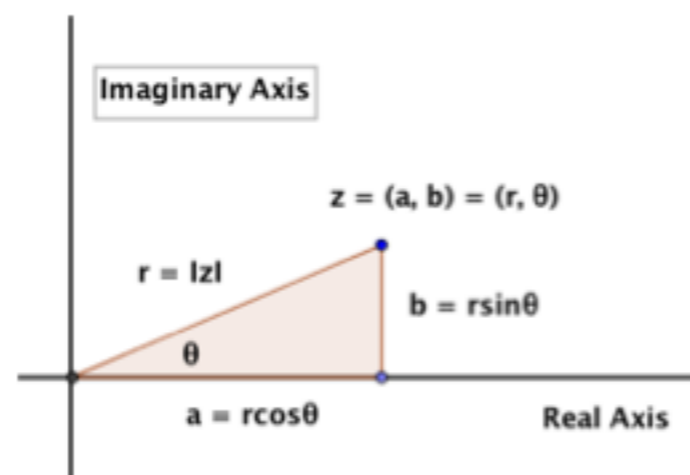
So the complex number $-2 + 7i$ can be represented
 by the ordered pair $(-2, 7)$. Its graph is shown here:

Rectangular Coordinates	Rectangular Form
$(-2, 7)$	$-2 + 7i$

Graph the following complex numbers on the complex number plane given:



<u>Rectangular Form</u> <u>Coordinates</u>	<u>Rectangular</u> <u>Coordinates</u>
1. Plot $3+2i$	$(3, 2)$
2. Plot $4-i$	$(4, -1)$
3. Plot $-5i$	$(0, -5)$
4. Plot 8	$(8, 0)$
$a + bi$	(x, y)



The point representing the complex number can also be expressed in polar coordinates, (r, θ) .

Polar Coordinates

(r, θ)

$$x = r \cos \theta$$

$$y = r \sin \theta$$

Polar Form

$$r \cos \theta + (r \sin \theta)i$$

$$a + bi$$

Polar form of a complex number is long, so it is often abbreviated in the following way:

$$r \cos \theta + (r \sin \theta)i$$

$$r(\cos \theta + i \sin \theta)$$

$$rcis \theta \quad (r, \theta)$$

For example the polar form $\sqrt{2}cis45^\circ$ is an abbreviation for $\sqrt{2}(\cos 45^\circ + i \sin 45^\circ)$.

The corresponding polar coordinates would be $(\sqrt{2}, 45^\circ)$.

The length of the arrow representing the complex number z is called the **absolute value of z** . Using the Pythagorean Theorem $|z| = \sqrt{a^2 + b^2}$. Although points can be represented using both positive and negative r values, we will only use positive values of r in polar coordinates and polar form since $|z|$ is defined to be positive.

$$z = a + bi$$

$$= r cis \theta$$

$$|z| = \sqrt{a^2 + b^2}$$

Converting between polar and rectangular form:

5. Convert $1+i\sqrt{3}$ to polar form.

$$x = 1$$

$$y = \sqrt{3}$$

$$r^2 = x^2 + y^2$$

$$r = \sqrt{1 + 3} = 2$$

$$\tan \theta = \frac{y}{x} = \sqrt{3}$$

$$\theta = 60^\circ$$

$$(2, 60^\circ)$$

$$r \operatorname{cis} \theta$$

$$2 \operatorname{cis} 60^\circ$$

6. Convert $9 \operatorname{cis} \frac{4\pi}{3}$ to rectangular form.

$$r = 9$$

$$\theta = \frac{4\pi}{3}$$

$$x = r \cos \theta$$

$$= 9 \cos \frac{4\pi}{3}$$

$$= 9 \left(-\frac{1}{2}\right) = -4.5$$

$$y = r \sin \theta$$

$$= 9 \sin \frac{4\pi}{3}$$

$$= 9 \left(-\frac{\sqrt{3}}{2}\right) = -\frac{9\sqrt{3}}{2}$$

$$\left(-4.5, -\frac{9\sqrt{3}}{2}\right)$$

$$a + bi$$

$$-4.5 - \frac{9\sqrt{3}}{2}i$$